

Constraint Acquisition

Nadjib Lazaar

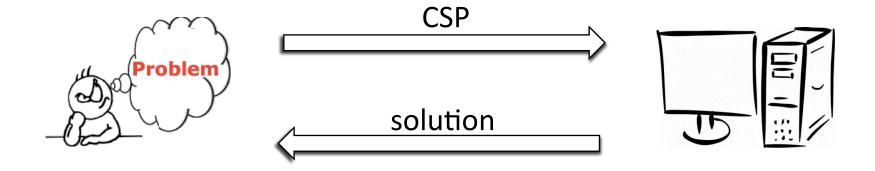


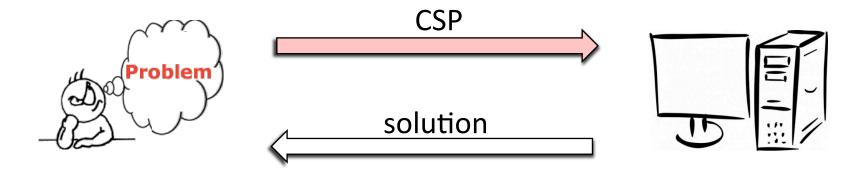
U. Montpellier, France LIRMM - COCONUT team

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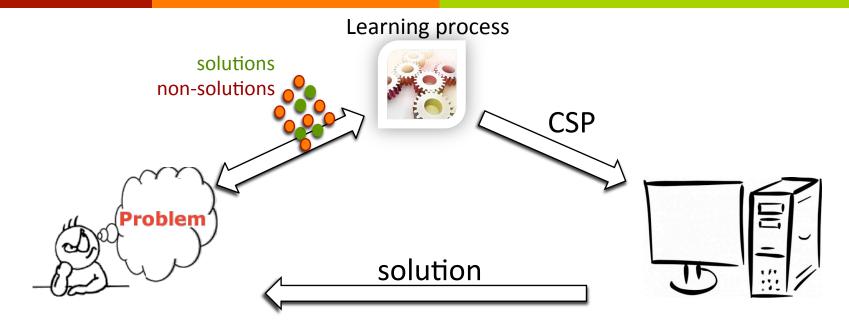




- Question: How does the user write down the constraints of a problem?
- Limitations: modelling constraint networks require a fair expertise

[Freuder99, Frisch et al.05, Smith06]

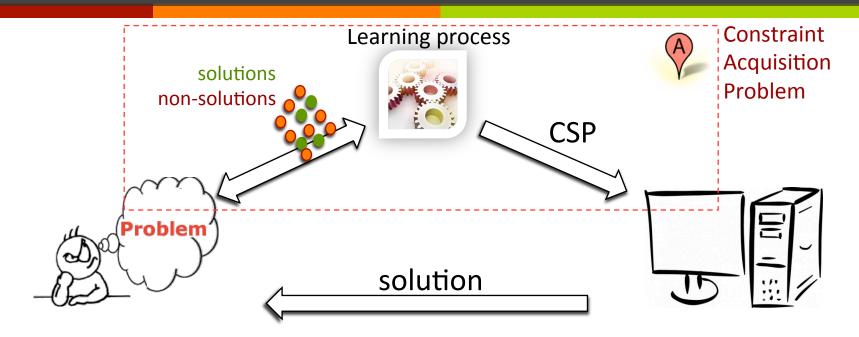
• Need: Simple way to build constraint model → Modeller-assistant



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- How: In a Machine Learning way (passive/active, offline/online, by reinforcement...)



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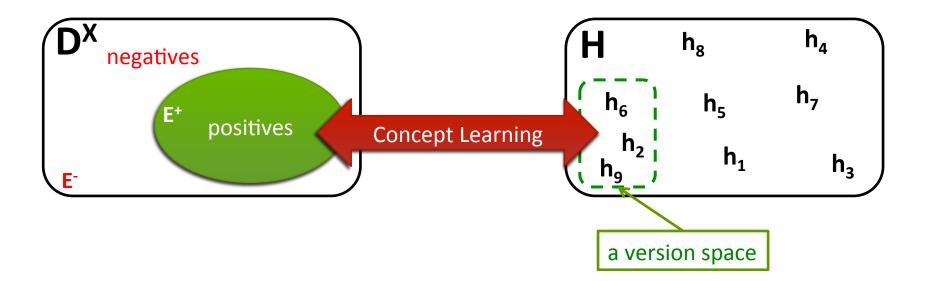
Version Space Learning (Overview) [Mitchell82]

- Let $X=x_1,...,x_n$ a set of attributes of domains $D=D_1,...,D_n$
- $m{\pi}$ A concept is a Boolean function $\,f:X o\{0,1\}\,$
 - $f(xi)=0 \Rightarrow xi$ is a negative instance
 - $f(xj)=1 \Rightarrow xj$ is a positive instance

Given a set of hypothesis H, any subset of H represents a version space

A concept to learn is the set of positive instances that can be represented by a version space

Version Space Learning (Overview) [Mitchell82]

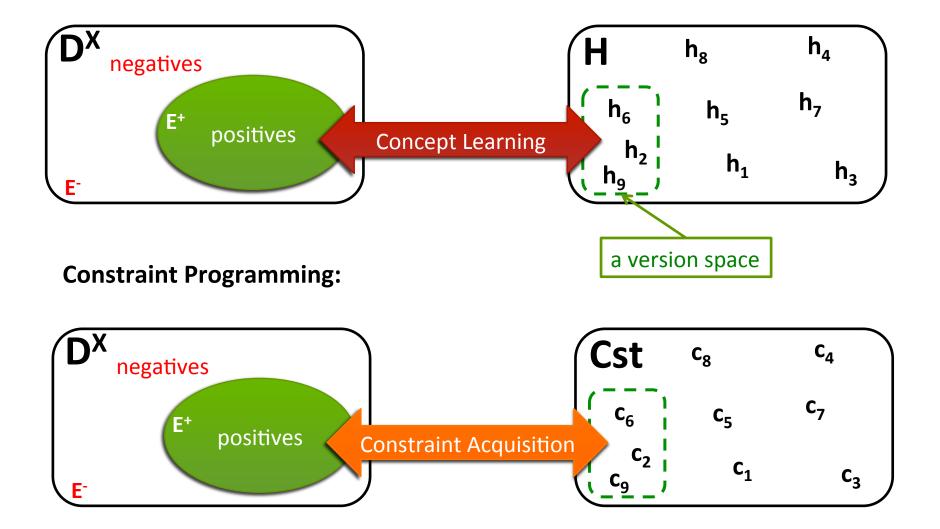


Concept to learn:

$$f: (\forall x_i \in E^+ : f(x_i) = 1) \land (\forall x_i \in E^- : f(x_i) = 0)$$

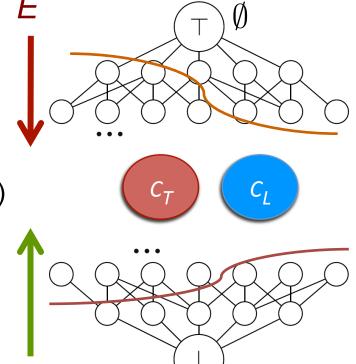
$$f \equiv h_2 \wedge h_6 \wedge h_9$$

Constraint Acquisition as Version Space Learning



Constraint Acquisition Problem

- Inputs:
 - **↗** (X,D): Vocabulary
 - Γ: Constraint language
 - → B: Bias (constraints/hypothesis)
 - **尽** C_T: Target Network (concept to learn)
 - **7** (E⁺,E⁻): training set
- Output:
- C_L: Learned network such that:



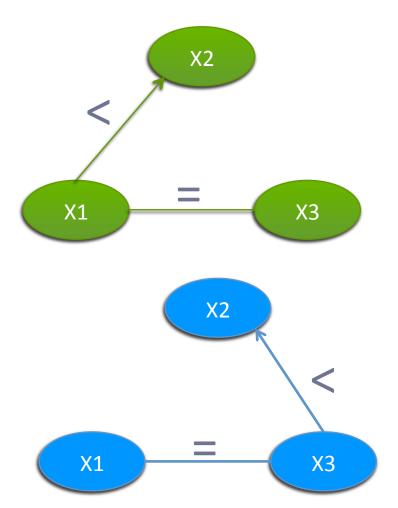
Convergence Pb:

 $(C_L \subset B) \land (\forall e_i \in E^+ : e_i \in sol(C_L)) \land (\forall e_i \in E^- : e_i \notin sol(C_L))$

coNP-complete [Constraint Acquisition, AIJ17]

Example

- $\bullet \ \Gamma = \{<, =\}$
- $\bullet B = \{x_i < x_j, x_i = x_j, \forall i, j\}$
- $C_T = \{x_1 = x_3, x_1 < x_2\}$
- $C_L = \{x_1 = x_3, x_3 < x_2\}$

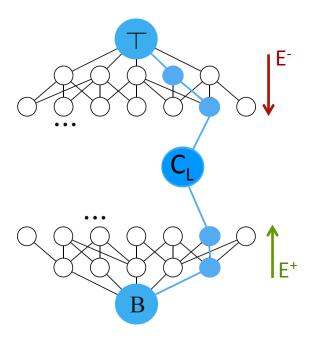


State of the art

- Matchmaker agents [Freuder and Wallace wAAAI97]
- CONACQ
 - SAT-Based constraint acquisition
 - Bidirectional search using Membership queries
 - Conacq1.0 (passive learning) [Bessiere et al. ECML05]
 - → Conacq2.0 (active learning) [Bessiere et al. IJCAI07]

$$\mathcal{K} = \underbrace{(\neg x_1 \land \neg x_2 \land \neg x_3)}_{\mathbf{e}^+} \bigwedge \underbrace{(x_4 \lor x_5 \lor x_6 \lor x_7)}_{\mathbf{e}^-} \dots$$

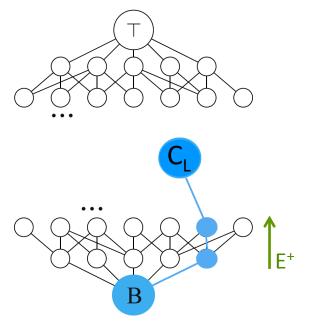
Argument based CONACQ [Friedrich et al.09]



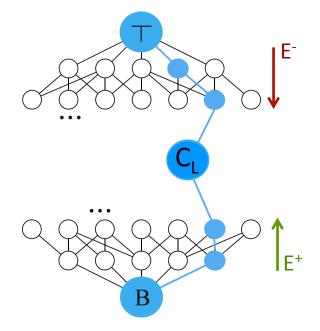
No-learnability using Membership queries [Constraint Acquisition, AIJ17]

State of the art

- ModelSeeker [Beldiceanu and Simonis, CP11'12]
 - A passive learning
 - Based on global constraint catalogue (≈1000)
 - Buttom-up search



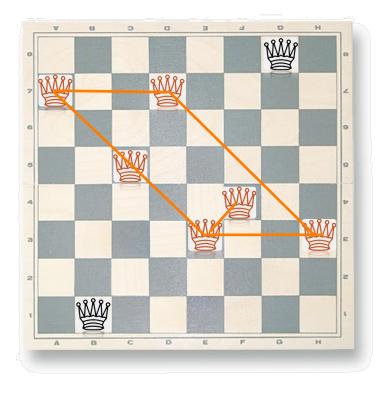
- **QUACQ** [Bessiere et al. IJCAI13]
 - Active learning approach
 - Bidirectional search
 - But it can be top-down search only if no positive example
 - Based on partial queries to elucidate the scope of the constraint to learn



Membership Queries

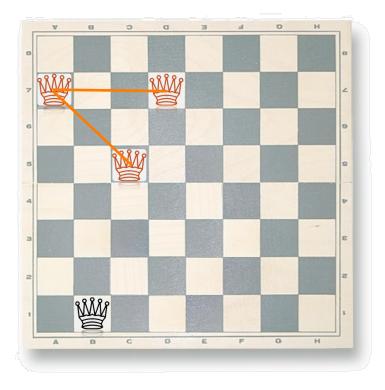


ask(2, 8, 4, 2, 6, 5, 1, 6)





ask(2, 8, 4, 2, 6, 5, 1, 6) = No

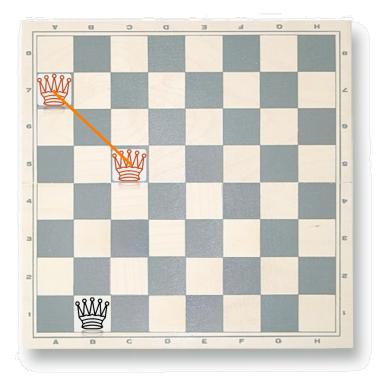




$$ask(2, 8, 4, 2, -, -, -, -) = No$$

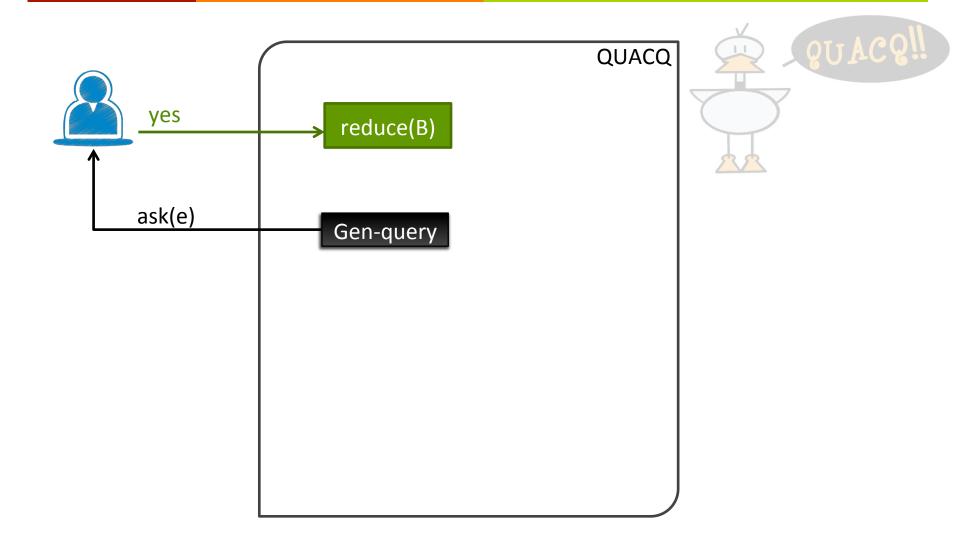


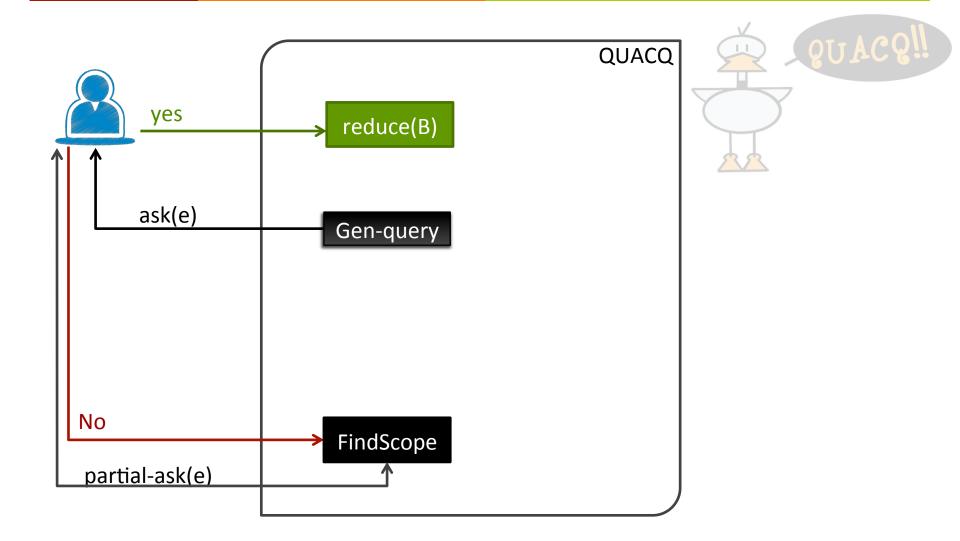


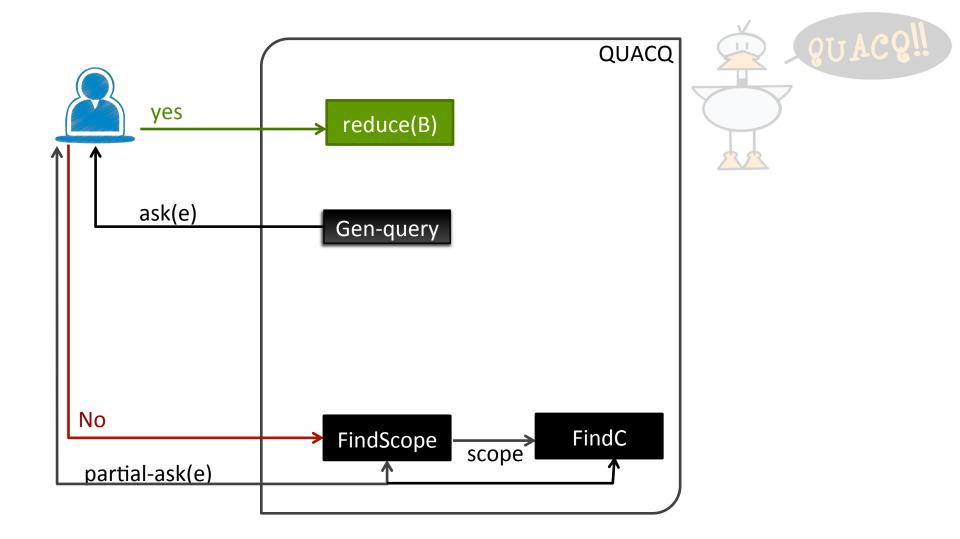


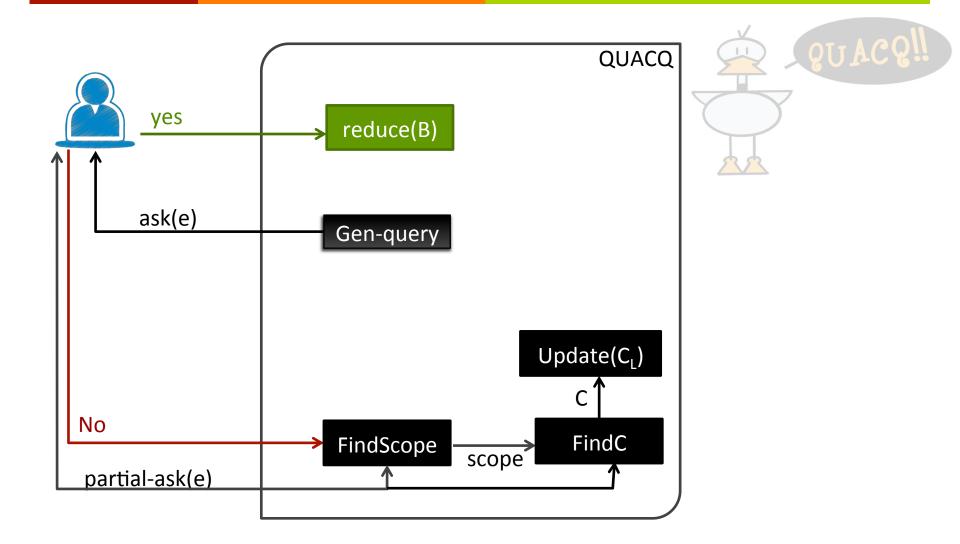


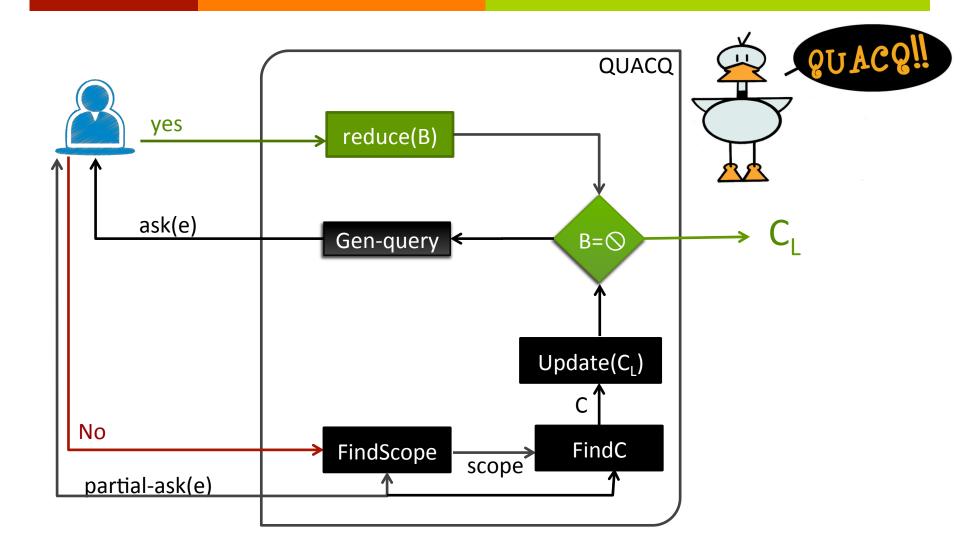
$$ask(2, 8, 4, -, -, -, -) = No$$











Algorithm 1: QUACQ: Acquiring a constraint network C_T with partial queries

```
1 C_L \leftarrow \varnothing;

2 while true do

3 | if sol(C_L) = \varnothing then return "collapse";

4 | choose e in D^X accepted by C_L and rejected by B;

5 | if e = nil then return "convergence on C_L";

6 | if ASK(e) = yes then B \leftarrow B \setminus \kappa_B(e);

7 | else

8 | c \leftarrow \texttt{FindC}(e, \texttt{FindScope}(e, \varnothing, X, \textbf{false}));

9 | if c = nil then return "collapse";

10 | else C_L \leftarrow C_L \cup \{c\};
```

Complexity of QUACQ

The number of queries required to find the target concept is in:

$$O(|C_T| \cdot (\log |X| + |\Gamma|))$$





Some Results

Sudoku

A target network on 81 variables with 810 constraints

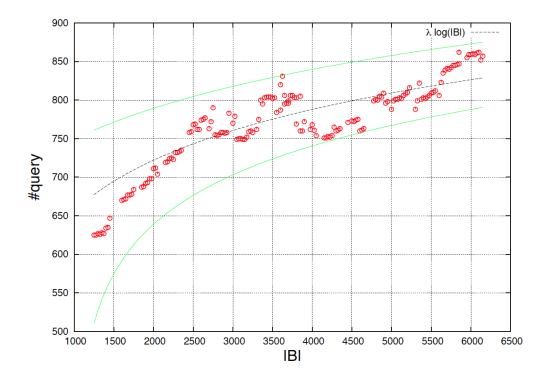
Bias of 19440 binary constraints

	$ C_L $	#q	$\#q_c$	$ar{q}$	time
Sudoku 9 × 9	810	8645	821	20.58	0.16

Experiments

Zebra puzzle

QUACQ behavior on different bias sizes



Conclusions

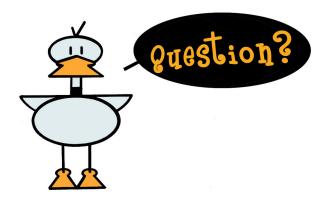
- QUACQ: new constraint acquisition approach based on partial queries
 - Active learning approach
 - Learning a constraint in a log scale of #queries
 - Queries are often much shorter than membership ones
 - Can follow a top-down search to learn a constraint network

Time left?



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In practice?

Limitation:

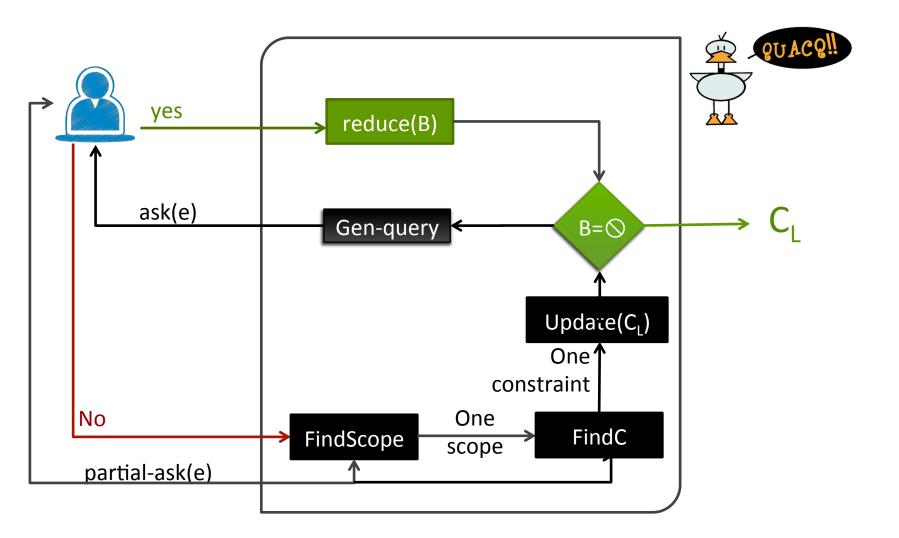
- Hard to put in practice:
 - QUACQ needs more than 8000 queries to learn the Sudoku model

Need:

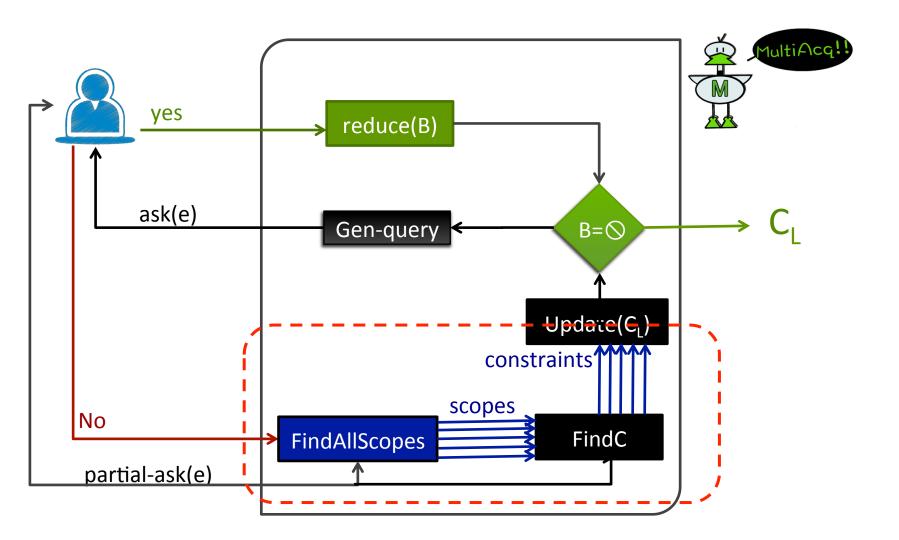
 Reduce the dialogue with the user to make constraint acquisition more efficient in practice

How:

 Eliciting more information on why a complete instantiation is classified as negative by the user



MULTIACO: Multiple Acquisition [IJCAI-W15]



MULTIACQ: Multiple Acquisition

e: Membership query

Q: Why the user said No?







[Bessiere et al., IJCAI13]

- FindScope function
- QuickXplain like function [Junker 04]
- Returns one scope (explanation)
- \rightarrow FindScope(e)=(X3,x5)
- → #learned constraint = 1



[Arcangioli et al., IJCAI16]

- FindAllScopes function
- CAMUS like function [Liffiton et al. 07]
- Returns all Minimal No Scopes (MUS in SAT)
- → FindAllScope(e)={(X1,x3), (X1,x4), (X3,x5), (X5,x6), (X5,x8),(X4,x8)}
- → #learned_constraint = 6

MNS: Minimal No Scope

Given a negative example e, an MNS is a subset of variables $U \subset X$ such that:

$$ASK(e_U) = no \text{ and } \forall x_i \in U : ASK(e_{U \setminus x_i}) = yes$$

7 Lemmas:

FindAllScopes function

INPUT: example e on (X1, X2, X3, X4) variables **OUTPUT:** MNS = (X1, X2), (X1, X3), (X2, X3, X4)

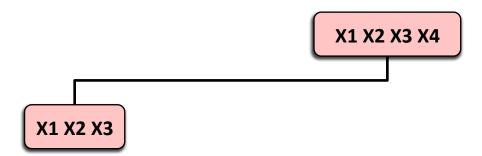
#Recusive calls	#ask
1	1

X1 X2 X3 X4

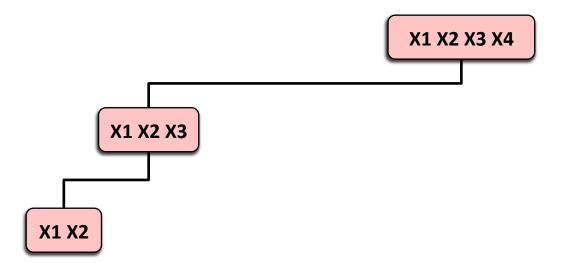
FindAllScopes function

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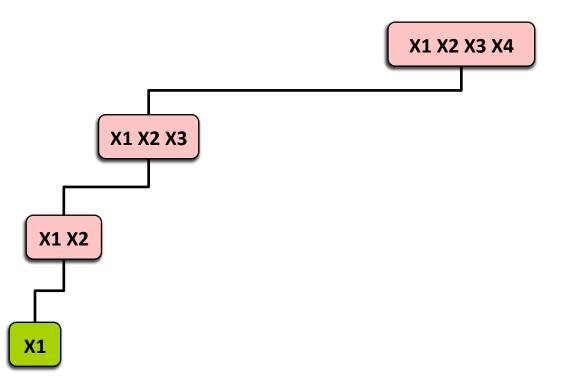
#Recusive calls	#ask
2	2



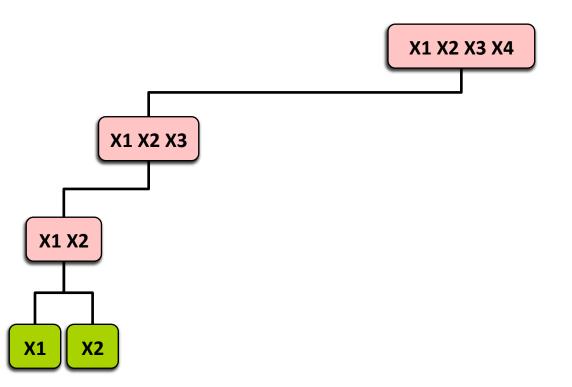
#Recusive calls	#ask
3	3



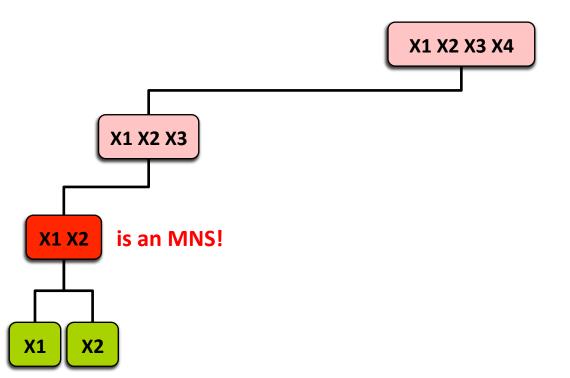
#Recusive calls	#ask
4	4



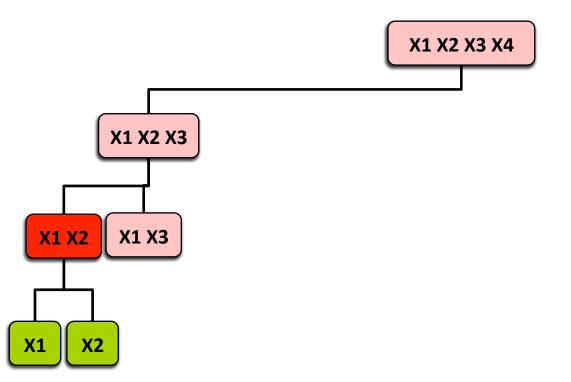
#Recusive calls	#ask
5	5



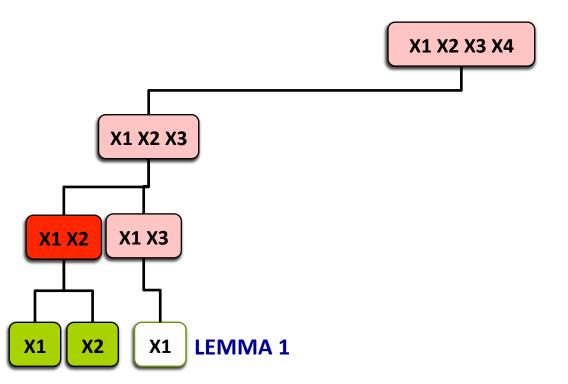
#Recusive calls	#ask
5	5



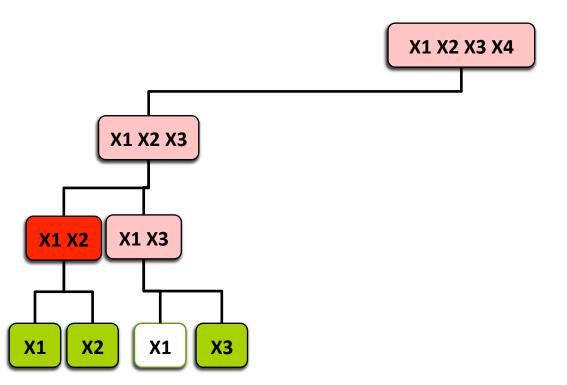
#Recusive calls	#ask
6	6



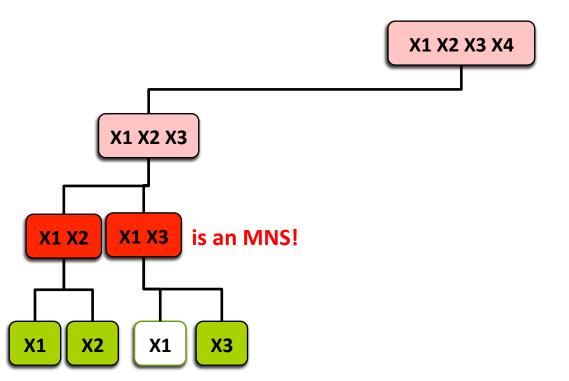
#Recusive calls	#ask
7	6



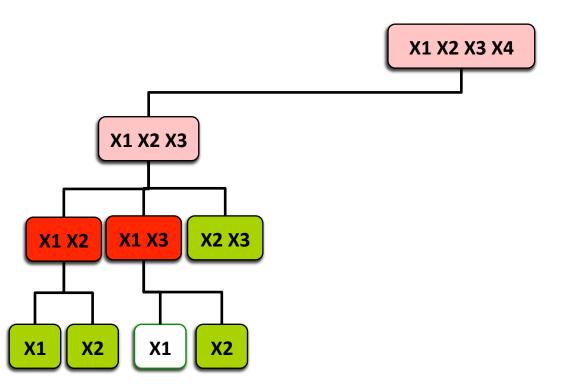
#Recusive calls	#ask
8	7



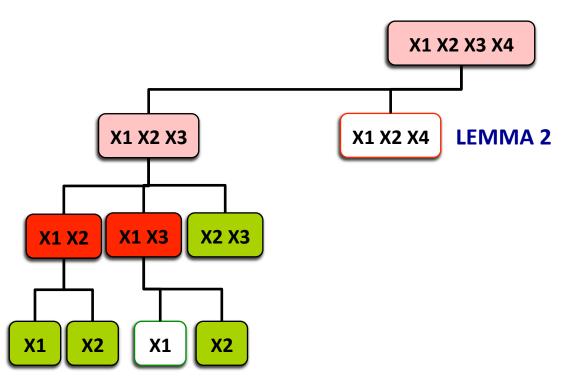
#Recusive calls	#ask
8	7



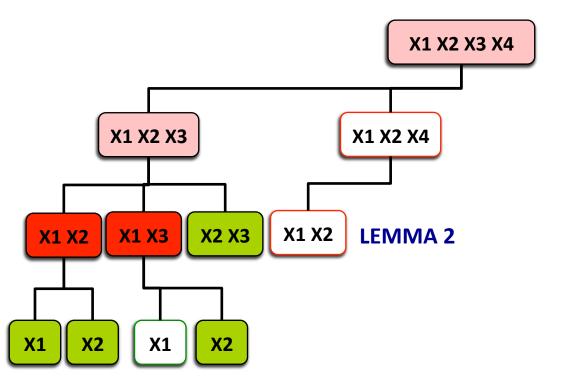
#Recusive calls	#ask
9	8



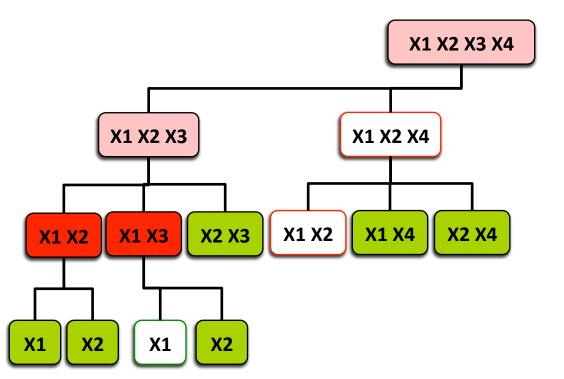
#Recusive calls	#ask
10	8



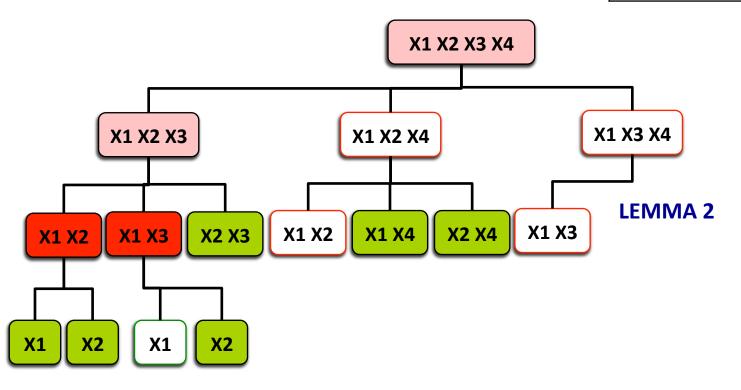
#Recusive calls	#ask
11	8



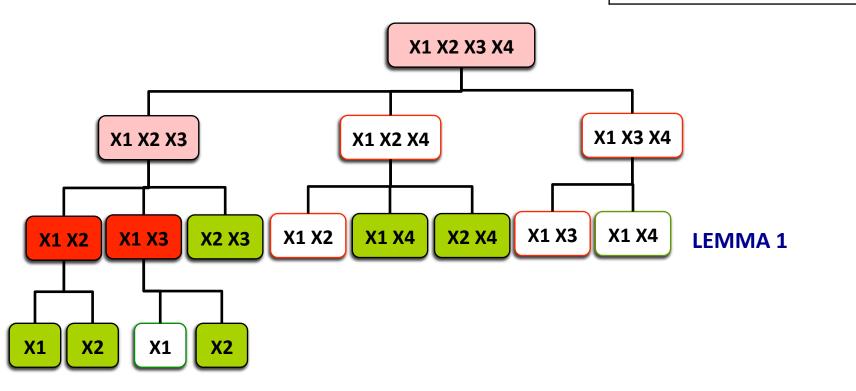
#Recusive calls	#ask
13	10



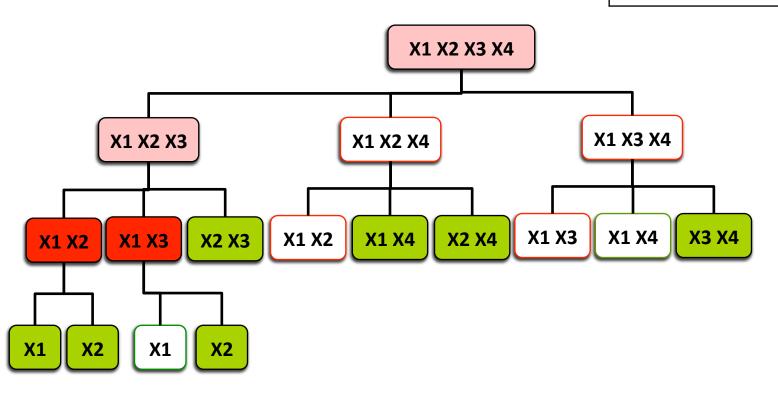
#Recusive calls	#ask
15	10



#Recusive calls	#ask
16	10



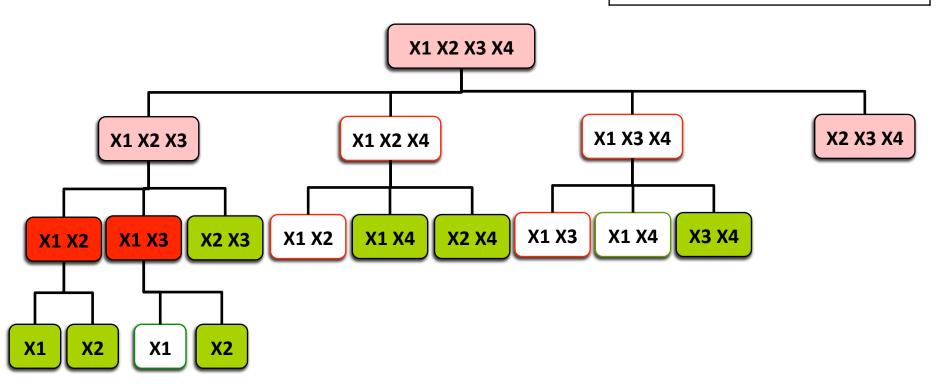
#Recusive calls	#ask
17	11



INPUT: example **e** on (X1, X2, X3, X4) variables

OUTPUT: MNS = (X1, X2), (X1, X3), (X2, X3, X4)

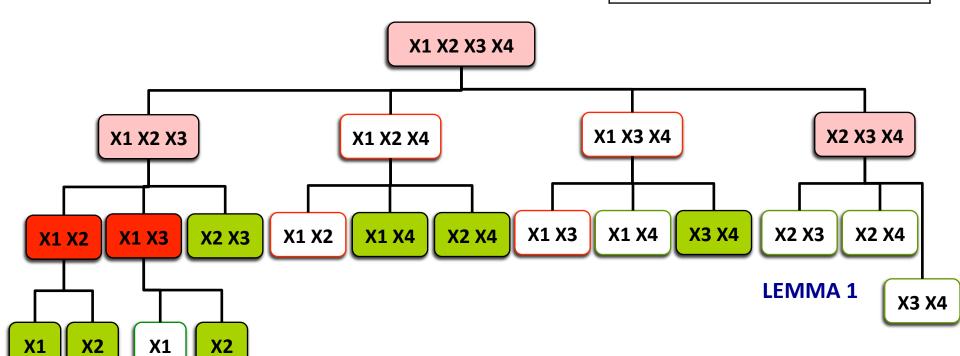
#Recusive calls	#ask
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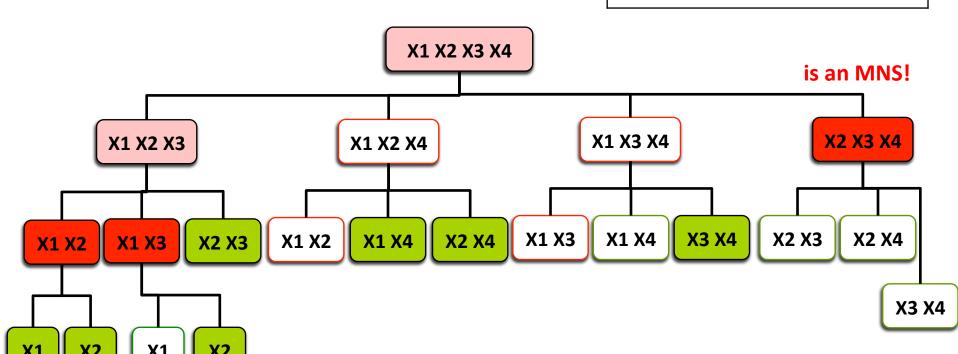
#Recusive calls	#ask
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#Recusive calls	#ask
21	12



Some Results

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Bias of 19440 binary constraints

	$ C_L $	#q	$\#q_c$	$ar{q}$	time
Sudoku 9 × 9	810	8645	821	20.58	0.16

MultiAcq → 3821 (gain 60%)

Conclusions

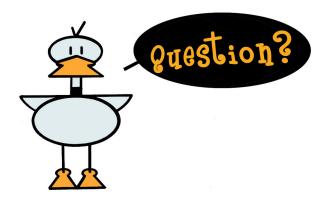
- QUACQ focuses on the scope of one constraint each time we give it a negative example
- MULTIACQ with its FindAllScopes function aims to report all minimal scopes of violated constraints
- **7** The results show:
 - MULTIACQ dramatically improves the basic version of QUACQ in terms of #queries
 - The queries are often much shorter
 - MULTIACQ can be time-consuming

Still time left?



Constraint Acquisition

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24-05-17 Nantes





In practice?

Limitation:

- Hard to put in practice:
 - QUACQ needs more than 8000 queries to learn the Sudoku model

Need:

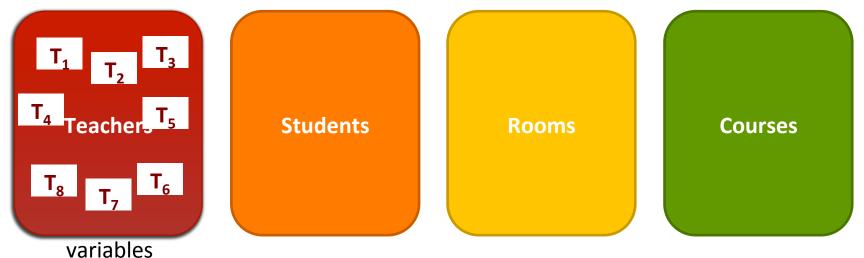
 Reduce the dialogue with the user to make constraint acquisition more efficient in practice

How:

- Eliciting more information on why a complete instantiation is classified as negative by the user → MULTIACQ [IJCAI16]
- Eliciting more information by asking complex queries to the user [ECAI14]

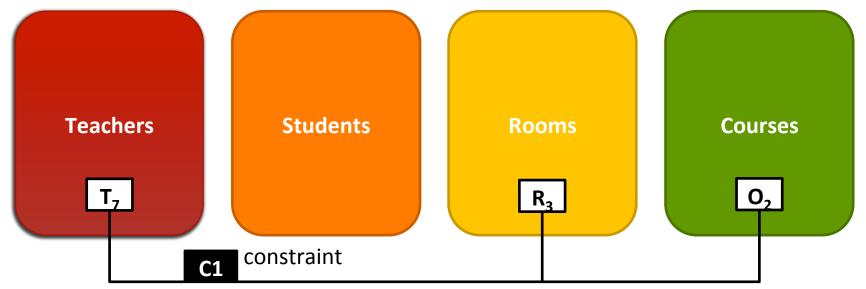
Variables and Types

- A type is a subset of variables defined by the user as having a common property
- Example (School Timetabling Problem)



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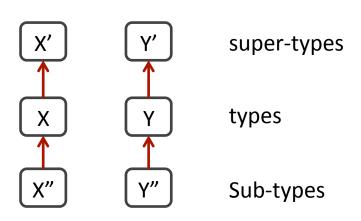
Can C1 be generalized to all Teachers, Rooms and Courses?

Generalization Query

- Let c(x,y) a learned constraint and X,Y are types of x,y:
 - Generalization Query: AskGen((X,Y),c)
- The user says yes iff the constraint c holds on all possible scope

$$(x_i, y_i) \in (X, Y)$$

Properties

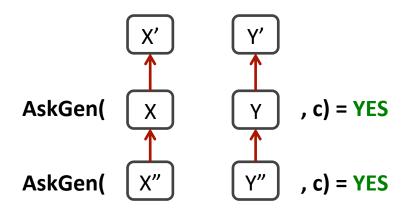


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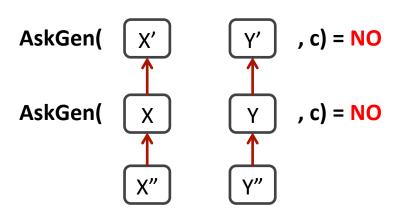


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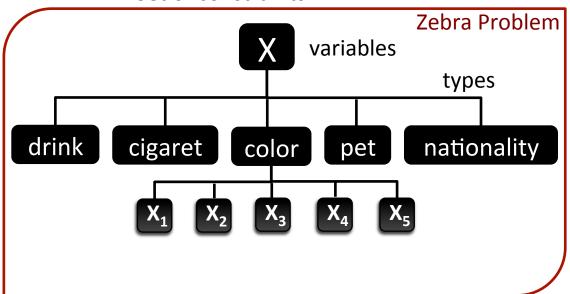
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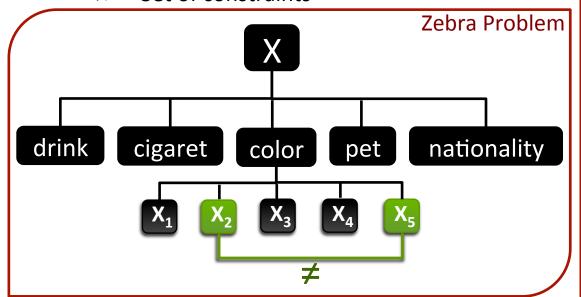
GENACO

- Inputs
 - A learned constraint
 - Combination of possible types (i.e., table)
- Output
 - Set of constraints



GENACQ

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INPUTS

- Learned constraint : X₂ ≠ X₅
- Table:

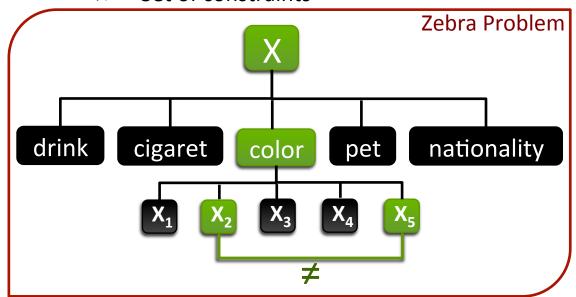
$$\#q = 0$$

askGer



GENACO

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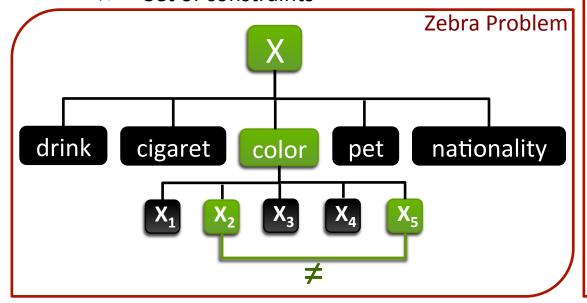


- Learned constraint : X₂ ≠ X₅
- Table:

#q = 1	X ₂	X ₅	
askGen	X_2	color	
	X ₂	Х	
	color	X ₅	
	color	color	
	color	Х	
	Х	X ₅	
	Х	color	
	Х	Х	

GENACQ

- Inputs
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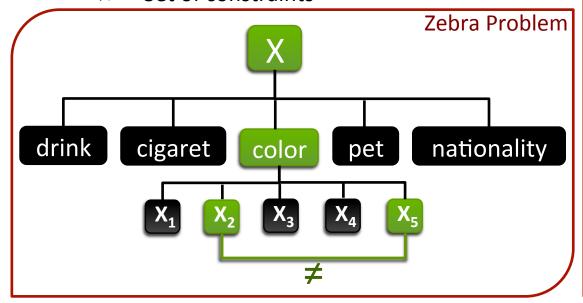


- Learned constraint : X₂ ≠ X₅
- Table:

			_
#q = 2	X ₂	X ₅	
	X_2	color	
skGen	X_2	Х	
	color	X ₅	
	color	color	
	color	Χ	×
	Х	X ₅	
	Х	color]
	Χ	Χ	×

GENACO

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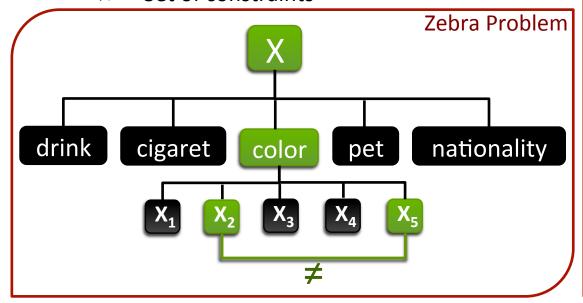


- Learned constraint : X₂ ≠ X₅
- Table:

#q = 3	X ₂	X ₅	
	X ₂	color	V
	X ₂	Х	
askGen	color	X ₅	V
	color	color	
	color	Χ	*
	X	X ₅	
	Χ	color	
	Х	Х	*

GENACO

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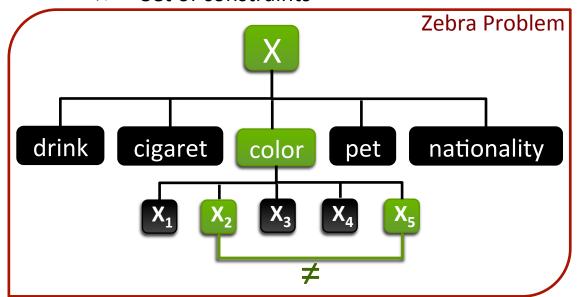


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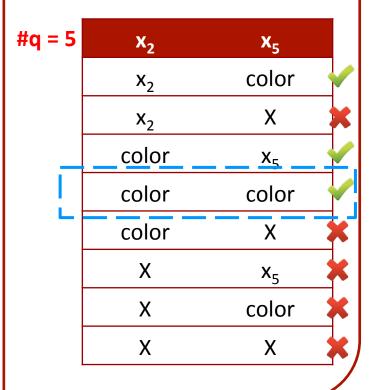
#q = 4	X ₂	X ₅	
	X_2	color	V
	X_2	Χ	×
	color	X ₅	
askGen	color	color	
	color	Χ	×
	X	X ₅	×
	Χ	color	×
	Х	Х	×

GENACQ

- Inputs
 - A learned constraint
 - Combination of possible types (i.e., table)
- Output
 - Set of constraints

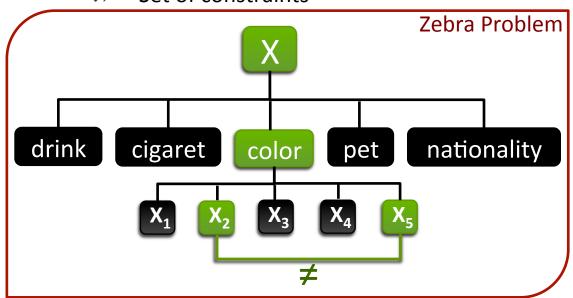


- Learned constraint : X₂ ≠ X₅
- Table:



GENACQ

- Inputs
 - A learned constraint
 - Combination of possible types (i.e., table)
- Output
 - Set of constraints

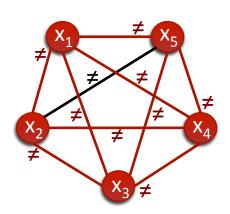


INPUTS

- Learned constraint : X₂ ≠ X₅
- Table

OUTPUT

• 9 constraints:



$$#q = 5$$

Results

	QUACQ	G-QUACQ		
	#Ask	#Ask	#AskGen	-
Zebra				50%
Sudoku				95%
Latin square		-		84%
RFLAP				88%
Purdey				34%

Conclusions

- Generalization query based on types of variables
- GENACQ algorithm
- Several heuristics and strategies to select the good candidate generalization query
- Can be plugged in any active constraint acquisition system
- Results by plugging GENACQ in the QUACQ acquisition System

Next step

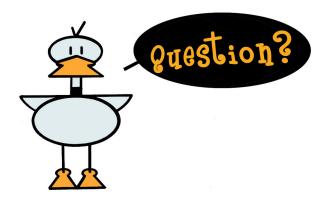
Detecting Types of Variables for Generalization [ICTAI15]

Still time left??



Constraint Acquisition

Nadjib Lazaar



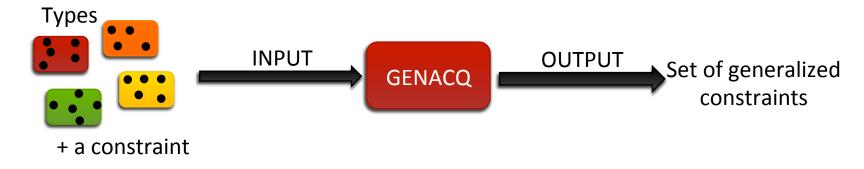
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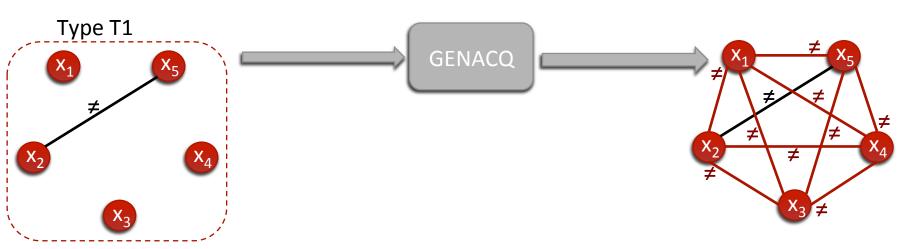




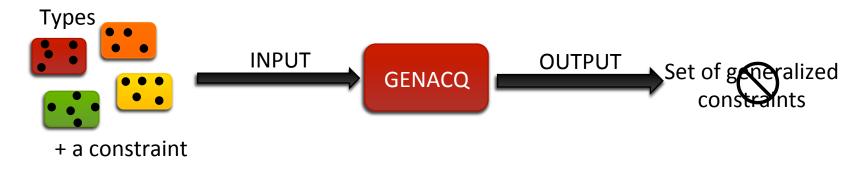
Motivations



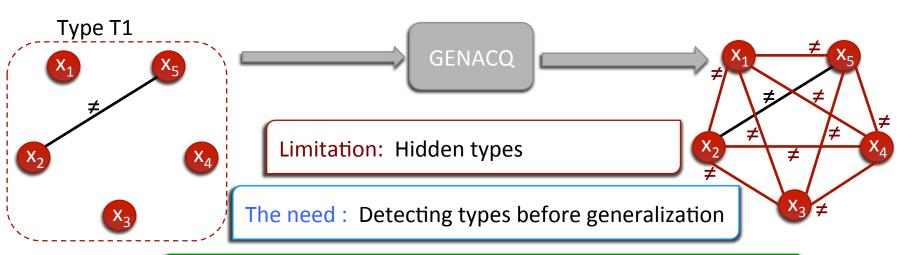
EXAMPLE



Motivations



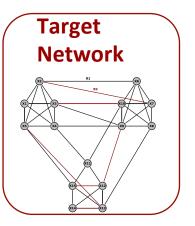
EXAMPLE

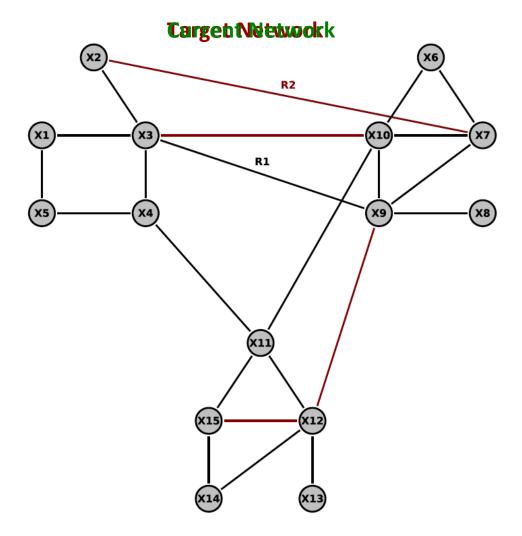


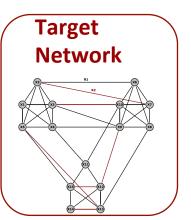
How: Reasoning on and mining the partial constraint graph

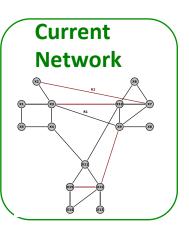
Detecting types of variables

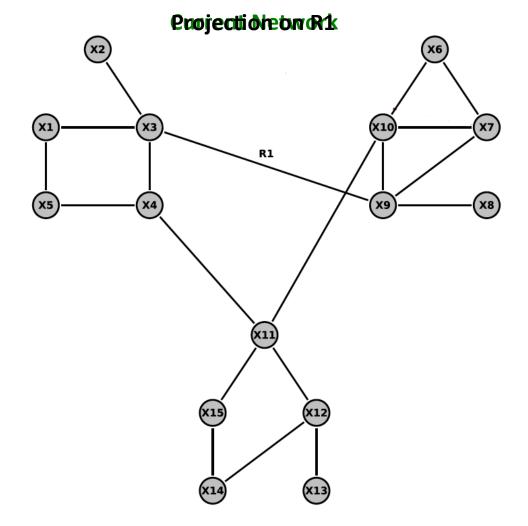
- ✓ Variables of the same type are often tightly connected with similar constraints
- Variables of different types are connected in a weaker way
- Detecting sub-graphs arose in the study of networks:
 - Social networks [Wasserman and Faust, 94]
 - Biochemical networks [Ito et al. 01]
- → Detecting community structures (types in our context)

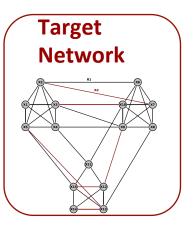


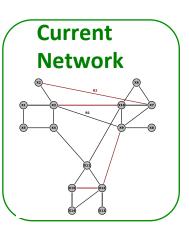


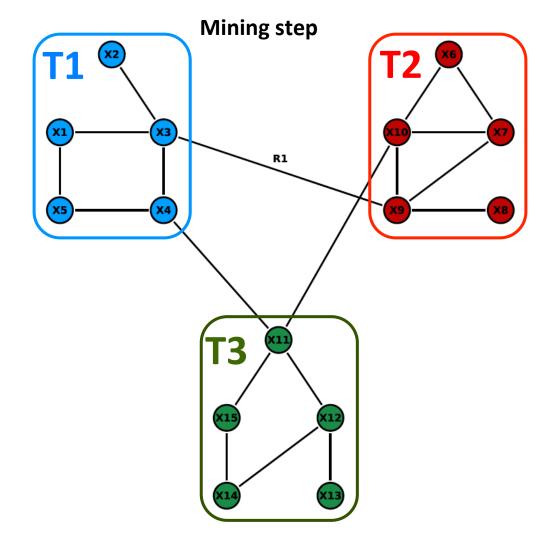


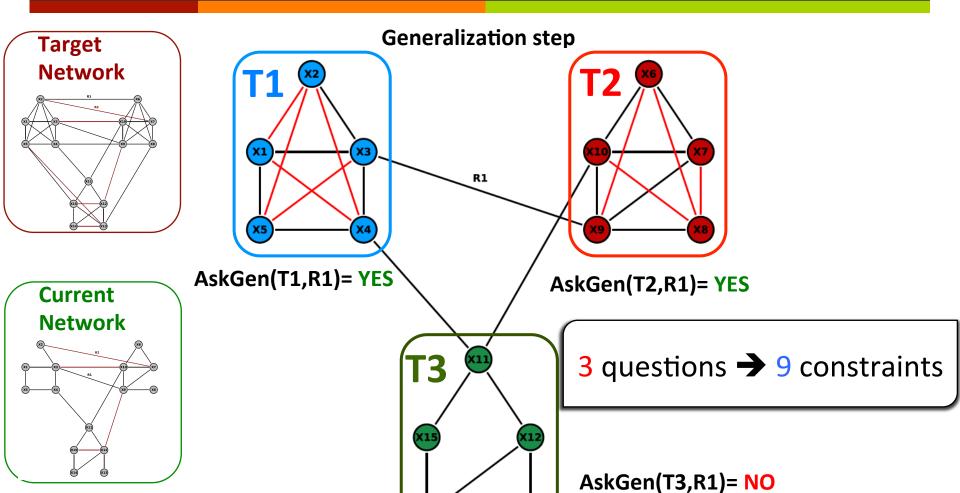






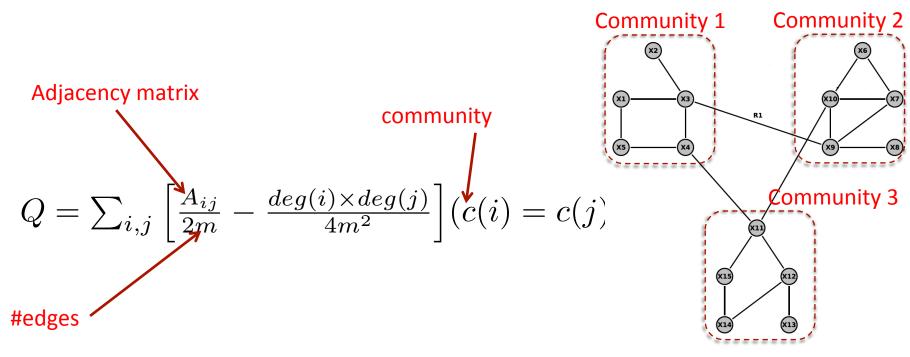






Mining the graph of learned constraints

Modularity optimization for communities detection [Newman and Girvan, 04]

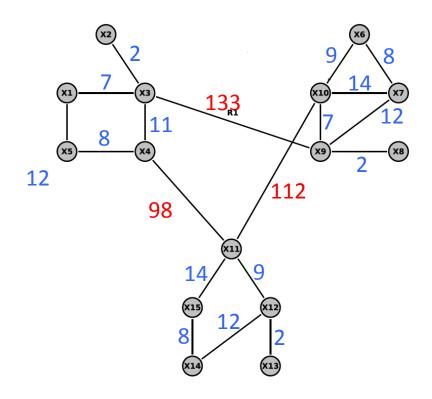


A high value of modularity Q correspond to a good partition

Mining the graph of learned constraints

- Modularity optimization for communities detection [Newman and Girvan, 04]
- Edge betweenness centrality [Girvan and Newman 02]

#paths through the edge e $B(e) = \sum_{ij} \frac{\sigma_{ij}(e)}{\sigma_{ij}}$ # shortest paths between i and j



Mining the graph of learned constraints

- Modularity optimization for communities detection [Newman and Girvan, 04]
- Edge betweenness centrality [Girvan and Newman 02]
- Quasi-cliques detection based on Bron Kerbosch's algorithm

[Bron and Kerbosch 73]

Experimental evaluation

- Mine&Ask is implemented and plugged in QUACQ system, leading to M-QUACQ version
- M-QUACQ is compared to the basic version of QUACQ and the G-QUACQ version including GENACQ Algorithm.
- We evaluate the three different extracting types methods:
 - Modularity
 - Betweenness
 - γ -clique

Some Results

	QUAcq	G-Ç	UAcq	M-QuAcq						
Strategies	#Ask	#Ask 7	#AskGen	AskGen # Ask # AskGen # no # yes						
Latin Square										
modularity				987	61	26	35			
betweenness	2058	129	68	1674	22	5	17	50%		
γ -clique				1172	35	1	34			
PlaceNumPuzzle										
modularity		_		627	35	4	31			
betweenness	3746	351	39	655	33	2	31	82 %		
γ -clique				688	33	2	31			
Murder										
modularity				272	12	2	10			
betweenness	483	230	55	272	12	2	10	41%		
γ -clique				342	13	3	10			

Some Results

	QuAcq	g-QuAcq		M-QUACQ						
Strategies	#Ask	#Ask	#AskGen	#Ask #Ask #Ask #Ask #Ask #Ask #Ask #Ask	eq AskGer	1 #no :	#yes			
Zebra										
modularity				410	14	0	14			
betweenness	694	257	67	410	14	0	14	40%		
γ -clique				410	14	0	14			
			Purdey							
modularity				140	8	0	8			
betweenness	205	93	39	140	8	0	8	27 %		
γ -clique				140	8	0	8			
Sudoku										
modularity				7963	57	20	37			
betweenness	9593	260	166	8960	50	18	32	16%		
γ -clique				9461	117	104	13			

Conclusions

- Mine&Ask algorithm able to mine partial graphs of constraints and to generalize constraints on potential types
- Used when no knowledge on variable types is provided
- Extracting potential types using:
 - ightharpoonup Modularity, betweeness, γ -clique
- M-QUACQ = Mine&Ask + QUACQ
 - → Next?
 - → More prediction and mining on partial constraint network for acquisition [IJCAI16]
 - Study on a time-bounded query generation [Ongoing work]



Constraint Acquisition

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